## The 2021 ICPC Greater NY Regional Contest

## G • Simple Collatz Sequence

The Simple Collatz Sequence (SCS) starting at an integer $\boldsymbol{n}$, is defined by the formula:

```
S(k)=(k/2 if k is even, else (k+1))
```

The sequence is then $\boldsymbol{n}, \mathrm{S}(\boldsymbol{n}), \mathrm{S}(\mathrm{S}(\boldsymbol{n})), \quad$... until the value first reaches 1 .
For example, starting at 11, we have:

$$
11->12->6->3->4->2->1
$$

The sequence always ends at 1. (Fun Fact: The Hard Collatz Sequence sends odd $k$ to $3 * k+1$. It is unknown whether that sequence always ends at 1.)

Let $A(\boldsymbol{n})=$ number of steps in the SCS starting at $\boldsymbol{n}$. For example, $\mathrm{A}(11)=6$.
Let $\mathrm{C}(\boldsymbol{n})=$ the number of integers $\boldsymbol{m}$ for which $\mathrm{A}(\boldsymbol{m})=\boldsymbol{n}$. For example, the integers for which $A(n)=6$ are:

10, 11, 13, 24, 28, 30, 31, 64
So C(6) $=8$.

Note that if $\boldsymbol{n}>2^{\boldsymbol{m}}$, then $\mathrm{A}(\boldsymbol{n})>\boldsymbol{m}$ since we need to divide by 2 at least $(\boldsymbol{m}+1)$ times.
Write a program to compute $\mathrm{C}(\boldsymbol{m})$.
(Continued on the next page.)

## Input

Input consists of a single line which contains a decimal integer, $\boldsymbol{m},(1<=\boldsymbol{m}<=40000)$, which is the value for which $C(\boldsymbol{m})$ is to be found.

## Output

The output consists of a single line that contains the value of $C(\boldsymbol{m})$ modulo 1000007 .
Sample 1:

| Sample Input | Sample Output |
| :--- | :--- |
| 6 | 8 |

Sample 2:

| Sample Input | Sample Output |
| :--- | :--- |
| 12345 | 540591 |

