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## The 2021 ICPC Greater NY Regional Contest

## E • How Many Unicycles in a Broken Wheel

(or Unicycle Returns)
A Wheel Graph of size $\boldsymbol{n}$ is a cycle of $\boldsymbol{n}$ vertices, $\mathrm{v}[1], \ldots, \mathrm{v}[\boldsymbol{n}]$ each of which is connected to a center vertex, v[0]. Examples of wheel graphs of size 4, 5, 6 and 8 are shown below:


A Broken Wheel Graph of size $\boldsymbol{n}$ is a wheel graph of size $\boldsymbol{n}$ with the edge from $\mathrm{v}[\boldsymbol{n}]$ to $\mathrm{v}[1]$ removed. Examples of broken wheel graphs of size 4, 5, 6 and 8 are shown below:


A spanning unicycle in a graph, $\mathbf{G}$, is a spanning tree in $\mathbf{G}$ with one additional edge added to form a single cycle. Each of the examples below is a spanning unicycle in a broken wheel graph of size 5:



Write a program to compute the number of different unicycles in a broken wheel graph of size $\boldsymbol{n}$. Recall that two subgraphs, $\mathbf{S} 1$ and $\mathbf{S 2}$, of a graph $\mathbf{G}$ are different if there is at least one edge of $\mathbf{G}$ that is in $\mathbf{S} 1$ and not in $\mathbf{S} 2$ OR an edge in $\mathbf{S 2}$ which is not in $\mathbf{S} 1$.

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## Input

Input consists of a single line that contains a decimal integer, $\boldsymbol{m}$ (3 <= $\boldsymbol{m}<=4000$ ), which is the size of the wheel graph to find the number of unicycles of.

## Output

The single output line consists of the count of unicycles modulo 100007.

| Sample Input | Sample Output |
| :--- | :--- |
| 5 | 19 |


| Sample Input | Sample Output |
| :--- | :--- |
| 1234 | 50380 |

