





**ICPC Greater NY Regional Contest** 

## **G** • Three Triangles

Starting with a  $\triangle ABC$  with vertices A, B, C and sides a, b, c opposite A, B, C, respectively:



Construct the altitudes **ha**, **hb** and **hc** to sides **a**, **b**, **c** respectively (red) and the perpendicular bisectors **pa**, **pb** and **pc** to sides **a**, **b**, **c** (green):



Let A' = hc intersect pb, B' = ha intersect pc and C' = hb intersect pa yeilding a new  $\Delta A'B'C'$  similar to ABC as shown on the next page.



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Finally, let **A**'' = reflection of **A**' in side **b**, **B**'' = reflection of **B**' in side **c** and **C**'' = reflection of **C**' in side **a** to obtain yet another similar triangle:



Write a program which takes as input the coordinates of the vertices **A**, **B** and **C** and outputs the areas of the three triangles.







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## Input

Input consists of a single line which contains three, space separated floating point values **Bx**, **Cx**, **Cy** in that order (-1.0 <= **Bx**, **Cx**, **Cy** <= 10.0).  $\triangle$ **ABC** will have area at least 1.0. The coordinates system is chosen so that **A** = (0, 0) is the origin and **B** = (**Bx**, 0) lies on the **X**-axis. **C** = (**Cx**, **Cy**) is arbitrary.

## Output

The output consists of a single line that contains three space separated floating point values to 4 decimal places. Area( $\Delta ABC$ ), Area( $\Delta A'B'C'$ ) and Area( $\Delta A'B'C'$ ) in that order.

Sample 1:

Sample Input	Sample Output
4.0 5.00 3.000	6.0000 4.8750 10.8750