



## D • Recursively Palindromic Partitions

A *partition* of a positive integer  $N$  is a sequence of integers which sum to  $N$ , usually written with plus signs between the numbers of the partition. For example

$$15 = 1+2+3+4+5 = 1+2+1+7+1+2+1$$

A partition is *palindromic* if it reads the same forward and backward. The first partition in the example is *not* palindromic while the second is. If a partition containing  $m$  integers is palindromic, its left half is the first  $\lfloor m/2 \rfloor$  integers and its right half is the last  $\lfloor m/2 \rfloor$  integers (which must be the reverse of the left half. ( $\lfloor x \rfloor$  is the greatest integer less than or equal to  $x$ .)

A partition is *recursively palindromic* if it is palindromic and its left half is recursively palindromic or empty. Note that every integer has at least two recursively palindromic partitions one consisting of all ones and a second consisting of the integer itself. The second example above is also recursively palindromic.

For example, the recursively palindromic partitions of 7 are:

$$7, 1+5+1, 2+3+2, 1+1+3+1+1, 3+1+3, 1+1+1+1+1+1+1$$

Write a program which takes as input an integer  $N$  and outputs the number of recursively palindromic partitions of  $N$ .

### Input

The first line of input contains a single integer  $N$ , ( $1 \leq N \leq 1000$ ) which is the number of data sets that follow. Each data set consists of a single line of input containing a single positive integer for which the number of recursively palindromic partitions is to be found.

### Output

For each data set, you should generate one line of output with the following values: The data set number as a decimal integer (start counting at one), a space and the number of recursively palindromic partitions of the input value.

Sample Input	Sample Output
3	1 4
4	2 6
7	3 60
20	